

# **Linear Algebra**

Berlin Chen

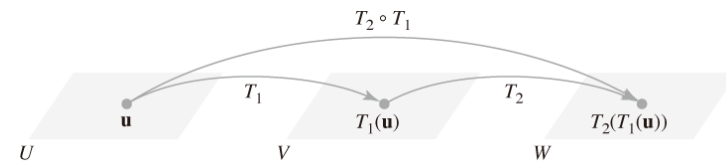
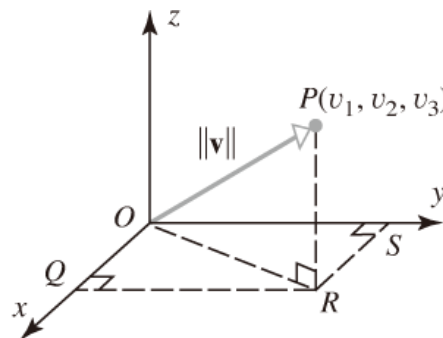
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# Linear Algebra (LA)

- Linear algebra is a branch of mathematics and continues to figure prominently in computer science and electrical engineering
  - Computation, geometry, theory, practical applications, to name just a few
- Simply put, linear algebra is the study of vectors, matrices, vector spaces and linear transformations

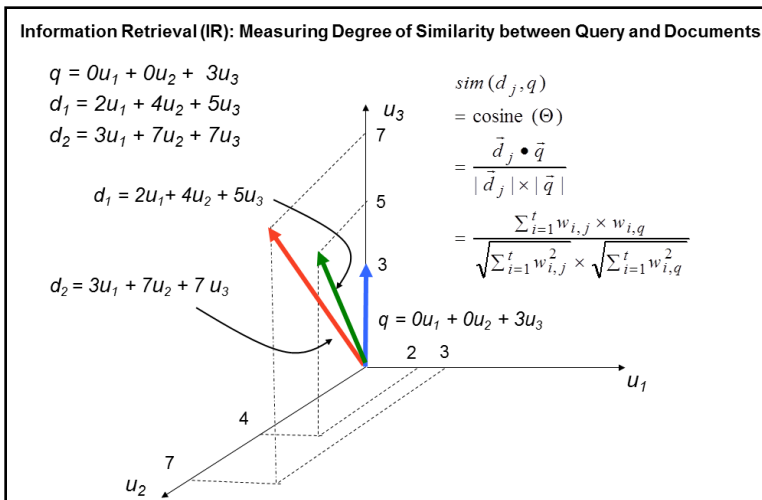
$$\begin{aligned}
 a_{11}x_1 + a_{12}x_2 + \cdots + a_{1n}x_n &= b_1 \\
 a_{21}x_1 + a_{22}x_2 + \cdots + a_{2n}x_n &= b_2 \\
 \vdots & \\
 a_{m1}x_1 + a_{m2}x_2 + \cdots + a_{mn}x_n &= b_m
 \end{aligned}$$

$$\begin{bmatrix}
 a_{11} & a_{12} & \cdots & a_{1n} & b_1 \\
 a_{21} & a_{22} & \cdots & a_{2n} & b_2 \\
 \vdots & \vdots & & \vdots & \vdots \\
 a_{m1} & a_{m2} & \cdots & a_{mn} & b_m
 \end{bmatrix}$$



# Main Objectives

- Develop the definitions, concepts and theories associated with linear algebra
  - Fundamentals: vectors operations, matrices operations, determinants, Euclidean vector spaces, linear systems, etc.
  - Advanced topics: matrix diagonalization, matrix factorization, linear transforms, numerical methods, practical applications, etc.
- Learn to make effective use of linear algebra in dealing with practical issues of interest
  - E.g., multimedia (text, speech, music and image) processing

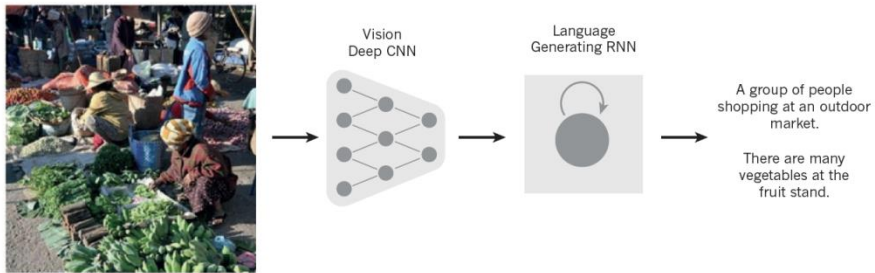


- Start with a matrix describing the intra- and Inter-document statistics between all terms and all documents
- Singular value decomposition (SVD) is then performed on the matrix to project all term and document vectors onto a reduced latent topical space

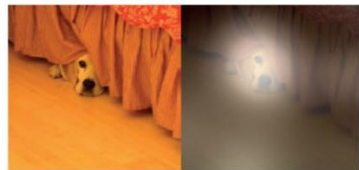
$\|A\|_F^2 = \sum_{i=1}^m \sum_{j=1}^n a_{ij}^2 \Rightarrow \|A\|_F^2 = \sigma_1^2 + \sigma_2^2 + \dots + \sigma_r^2 ?$

- In the context of information retrieval (IR), matching between queries and documents can be carried out in this topical space

# LA for Representation Learning



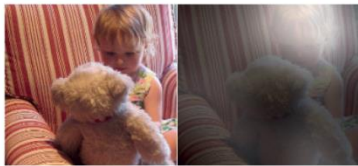
A woman is throwing a **frisbee** in a park.



A **dog** is standing on a hardwood floor.



A **stop** sign is on a road with a mountain in the background



A little **girl** sitting on a bed with a teddy bear.

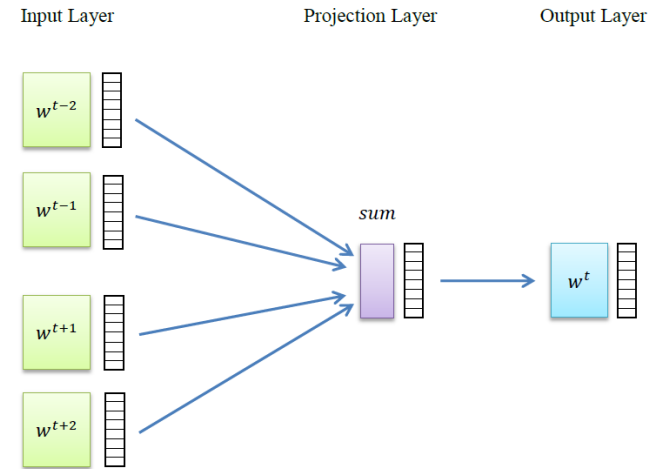


A group of **people** sitting on a boat in the water.



A giraffe standing in a forest with **trees** in the background.

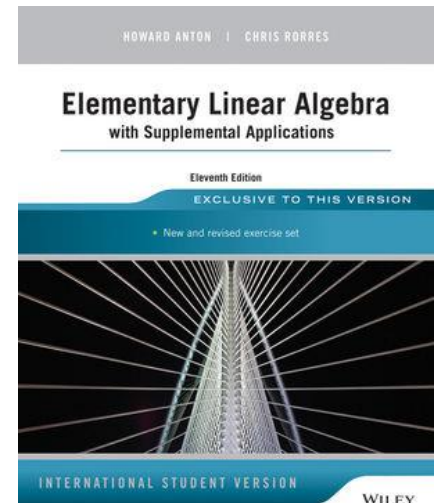
## Image to Text



## Word Prediction

# Textbook & Course Website

- H. Anton, C. Rorres, *Elementary Linear Algebra with Supplemental Applications*, 11<sup>th</sup> edition, Wiley, 2014



– Website

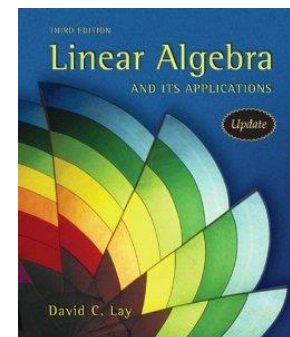
<http://www.wiley.com/WileyCDA/WileyTitle/productCd-1118677455.html>

- Course Website

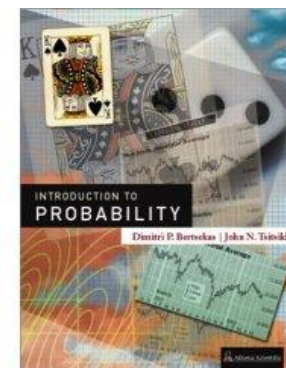
[http://berlin.csie.ntnu.edu.tw/Courses/LinearAlgebra/2014F-LA\\_Main.htm](http://berlin.csie.ntnu.edu.tw/Courses/LinearAlgebra/2014F-LA_Main.htm)

# Reference Books

- D. C. Lay, *Linear Algebra and Its Applications, 3rd Updated Edition*, Addison Wesley, 2005
  - Website  
<http://www.laylinalgebra.com/>



- D. P. Bertsekas, J. N. Tsitsiklis, *Introduction to Probability, 2nd Edition*, Athena Scientific, 2008
  - Website  
<http://www.athenasc.com/probbook.html>



# Tentative Topic List

1.	Systems of Linear Equations and Matrices
2.	Determinants
3.	Euclidean Vector Spaces
4.	General Vector Spaces
5.	Eigenvalues and Eigenvectors
6.	Inner Product Spaces
7.	Diagonalization and Quadratic Forms
8.	Linear Transformations

# Grading (*Tentatively!*)

- Midterm and Final: 45%
- Quizzes ( $\geq 5$  times) and Homework: 45%
- Attendance/Other: 10%
  
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