

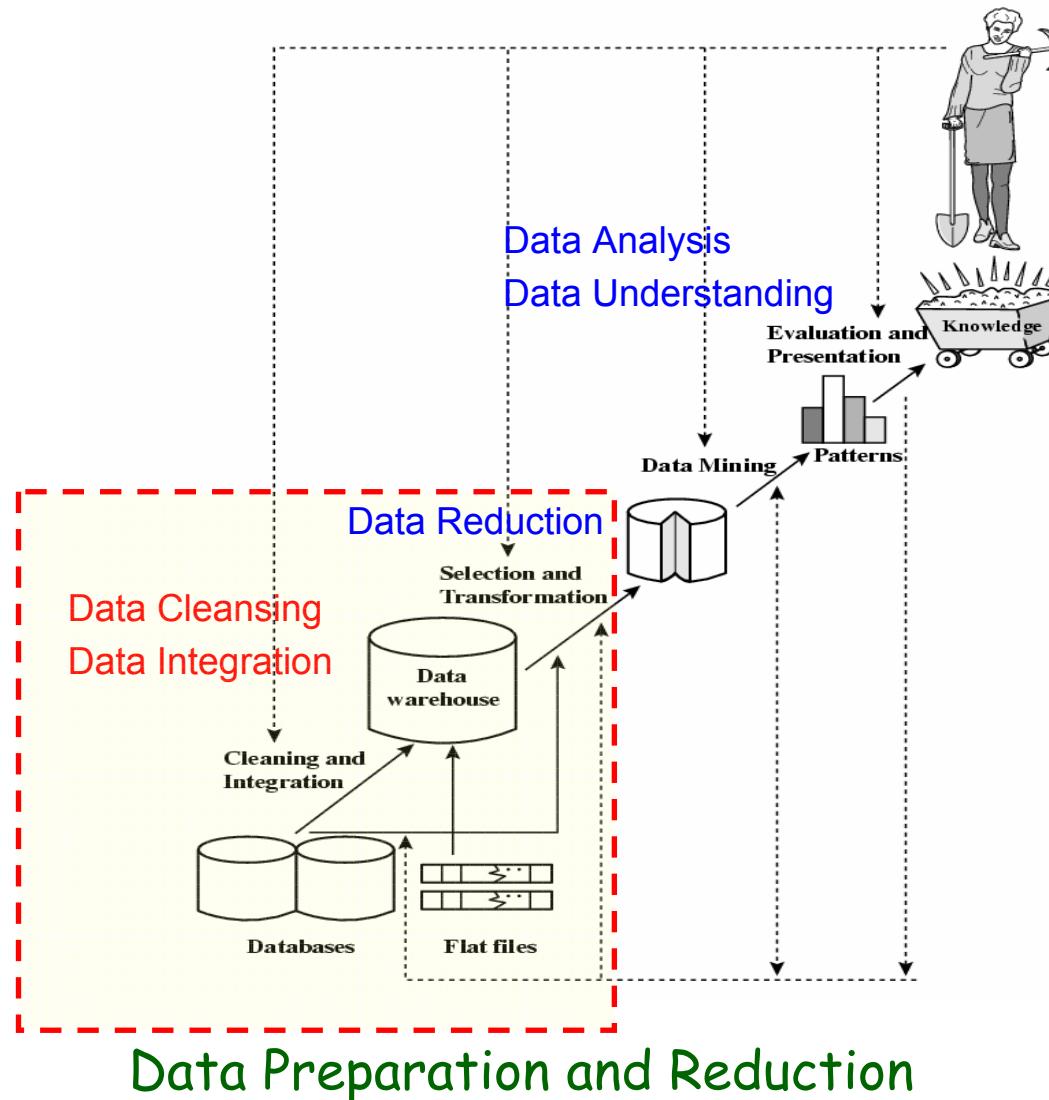
Data Preparation

Berlin Chen 2005

References:

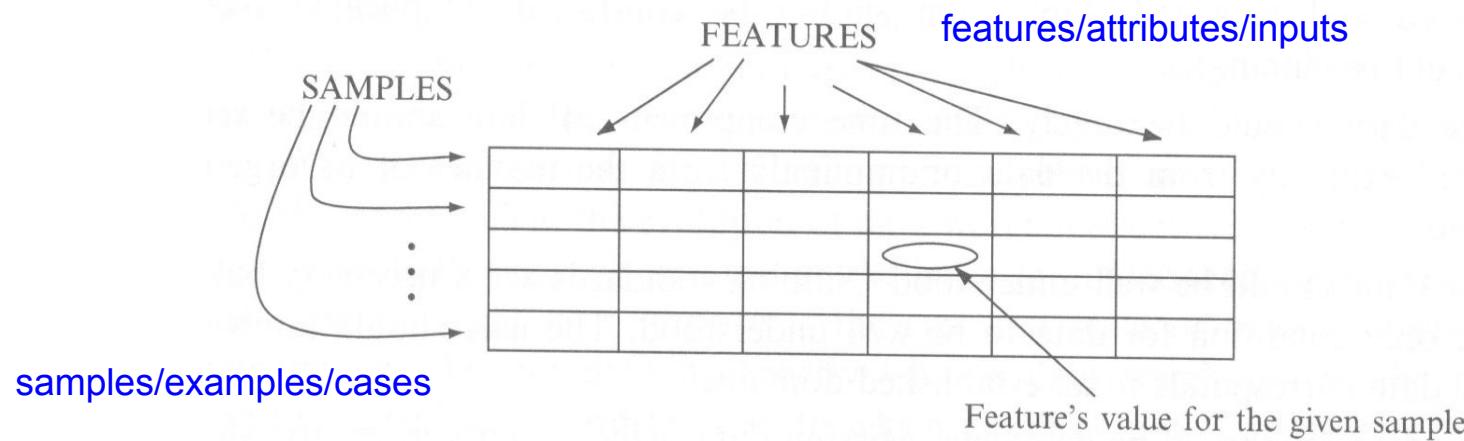
1. *Data Mining: Concepts, Models, Methods and Algorithms*, Chapters 2, 3
2. *Data Mining: Concepts and Techniques*, Chapters 3, 8

Where Are We Now ?



Data Samples

- Large amounts of samples with different types of features (attributes)
- Each sample is described with several features
 - Different types of values for every feature
 - Numeric: real-value or integer variables
 - Support “order” and “distance” relations
 - Categorical: symbolic variables
 - Support “equal” relation



Data Samples (cont.)

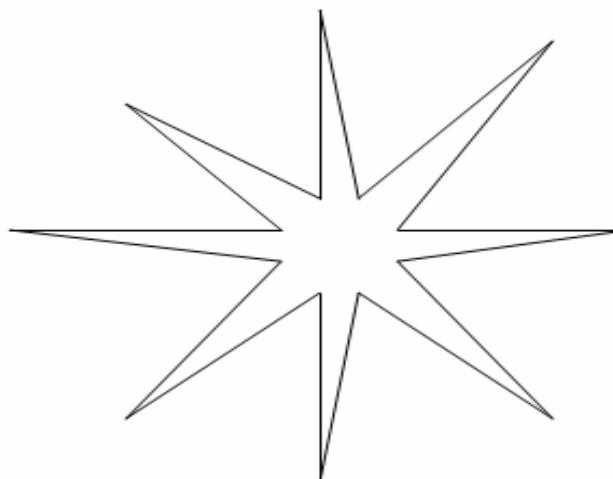
- Another way of classification of **variables**
 - Continuous variables
 - Also called *quantitative* or *metric* variables
 - Measured using interval or ratio scales
 - Interval: e.g., temperature scale
 - Ratio: e.g., height, length,... (has an absolute zero point)
 - Discrete variables
 - Also called *qualitative* variables
 - Measured using nonmetric scales (nominal, ordinal)
 - Nominal: e.g., (A,B,C, ...), (1,2,3, ...)
 - Ordinal: e.g., (young, middle-aged, old), (low, middle-class, upper-middle-class, rich), ...
 - A special class of discrete variable: **periodic variables**
 - Weekdays (Monday, Tuesday,...): distance relation exists

Data Samples (cont.)

- Time: one additional dimension of classification of data
 - Static data
 - Attribute values do not change with time
 - Dynamic (temporal) data
 - Attribute values change with time

Curse of Dimensionality

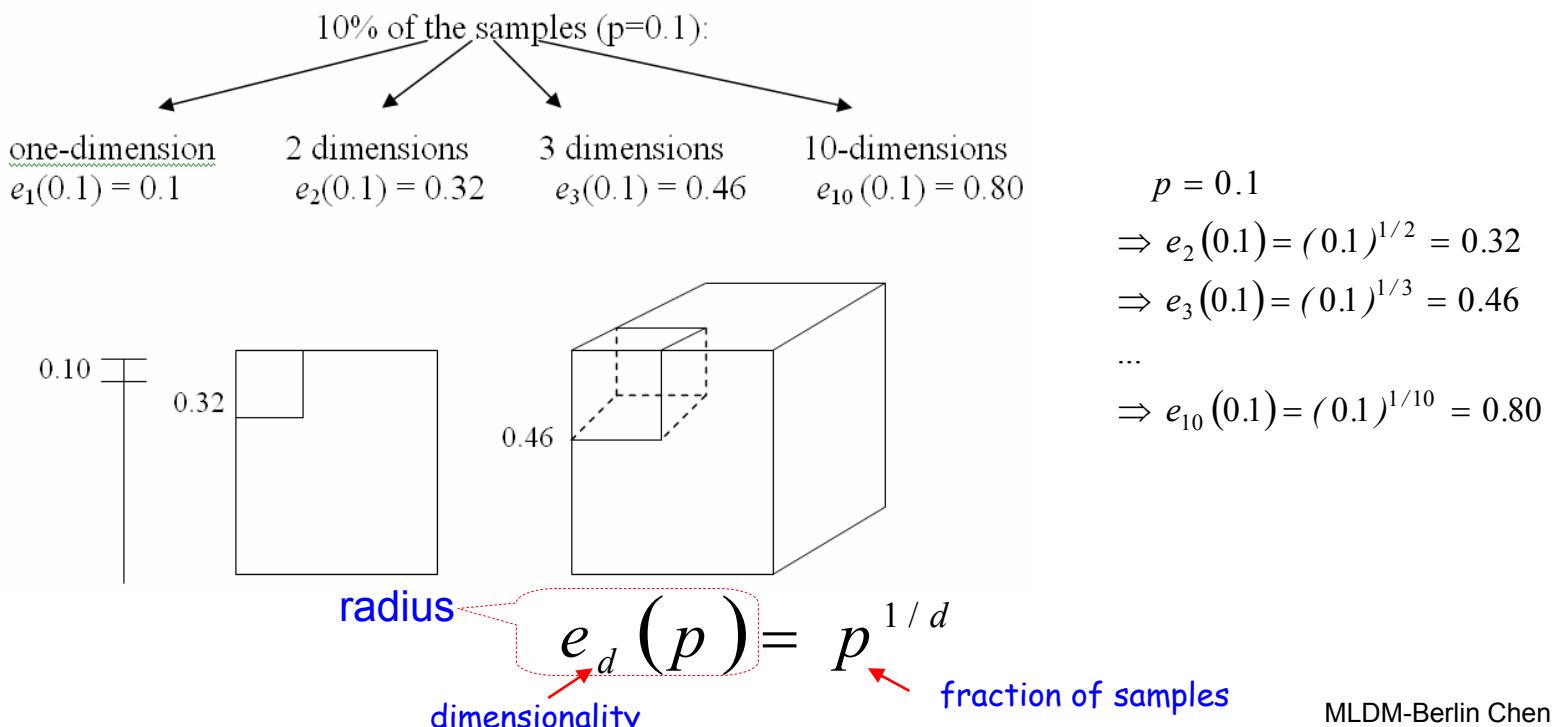
- Data samples are very often high dimensional
 - Extremely large number of measurable features
 - The properties of high dimensional spaces often appear **counterintuitive**
 - High dimensional spaces have a larger surface area for a given volume
 - Look like a porcupine after visualization



Curse of Dimensionality (cont.)

- Four important properties of high dimensional data
 - 1. The size of a data set yielding the same density of data points in an n -dimensional space increases exponentially with dimensions
 - 2. A large radius is needed to enclose a fraction of the data points in a high dimensional space

With the
same density

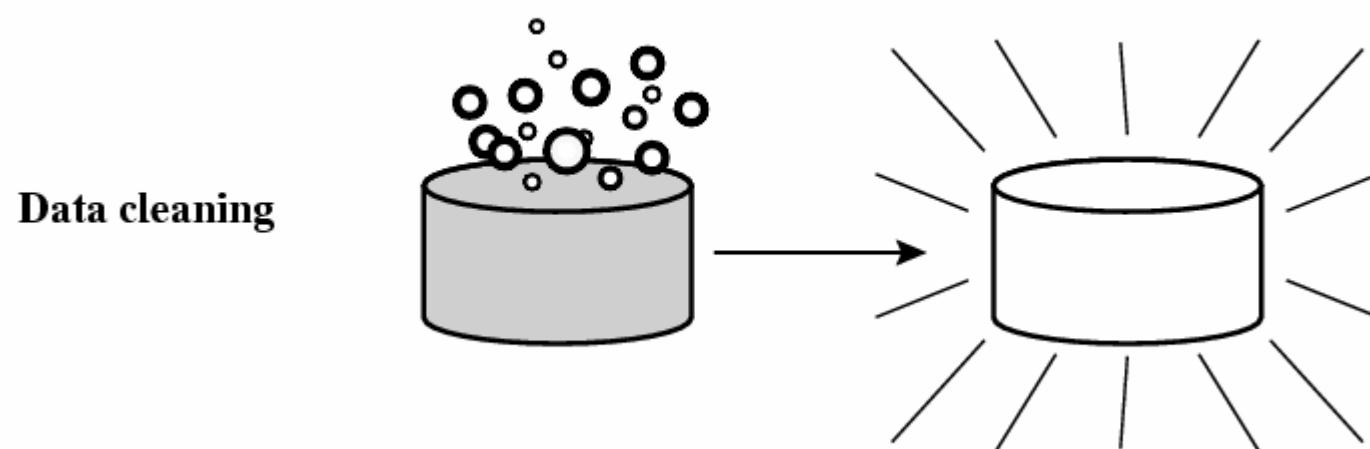


Curse of Dimensionality (cont.)

- With the
same number
of samples
- { 3. Almost every point is closer to an edge than to another sample point in a high dimensional space
 - 4. Almost every point is an outlier. The distance between the prediction point and the center of the classified points increases

Central Tasks for Data Preparation

- Organize data into a standard form that is ready for processing by data-mining and other computer-based tools
- Prepare data set that lead to the best data-mining performances



Sources for Messy Data

- Missing Values
 - Values are unavailable
- Misrecording
 - Typically occurs when large volumes of data are processed
- Distortions
 - Interfered by noise when recording data
- Inadequate Sampling
 - Training/test examples are not representative
-

Transformation of Raw Data

- Data transformation can involve the following
 - Normalizations
 - Data Smoothing
 - Differences and Ratios (attribute/feature construction)
 -

Attention should be paid to data transformation, because relatively simple transformations can sometimes be far more effective for the final performance !

Normalizations

- For data mining methods with examples represented in an n -dimensional space and distance computation between points, data normalization may be needed
 - Scaled values to a specific range, e.g., [-1,1] or [0,1]
 - Avoid overweighting those features that have large values (especially for distance measures)

1. Decimal Scaling:

- Move the decimal point but still preserve most of the original digital value

$$v'(i) = v(i)/10^k$$

for small k such that $\max(|v'|) < 1$

The feature value might concentrate upon a small subinterval of the entire range

$$\left. \begin{array}{l} \text{largest} = 455 \\ \text{smallest} = -834 \end{array} \right\} \Rightarrow k = 3$$

(-0.834 ~ 0.455)

$$\left. \begin{array}{l} \text{largest} = 150 \\ \text{smallest} = -10 \end{array} \right\} \Rightarrow k = 3$$

(-0.01 ~ 0.15)

Normalizations (cont.)

2. Min-Max Normalization:

- Normalized to be in [0, 1]

$$v'(i) = \frac{v(i) - \min(v)}{(\max(v) - \min(v))}$$

- Normalized to be in [-1, 1]

$$v'(i) = 2 \left[\frac{v(i) - \min(v)}{(\max(v) - \min(v))} - 0.5 \right]$$

- The automatic computation of min and max value requires one additional search through the entire data set
- It may be dominated by the outliers
- It will encounter an "out of bounds" error !

Normalizations (cont.)

3. Standard Deviation Normalization

- Also called *z-score* or *zero-mean* normalization
- The values of an attribute are normalized based on the mean and standard deviation of it
- Mean and standard deviation are first computed for the entire data set

$$v'(i) = \frac{v(i) - \text{mean}(v)}{\text{sd}(v)}$$

$$\bar{v} = \text{mean}(v) = \frac{\sum v}{n_v}$$
$$\sigma_v = \text{sd}(v) = \sqrt{\frac{\sum (v - \bar{v})^2}{n_v - 1}}$$

- E.g., the initial set of values of the attribute $v = \{1, 2, 3\}$ has

$$\text{mean}(v) = 1, \text{sd}(v) = 1 \text{ and new set of } v' = \{-1, 0, 1\}$$

Normalizations (cont.)

- An identical normalization should be applied both on the observed (training) and future (new) data
 - The normalization parameters must be saved along with a solution

Data Smoothing

- Minor differences between the values of a feature (attribute) are not significant and may degrade the performance of data mining
 - They may be caused by noises
- Reduce the number of distinct values for a feature
 - E.g., round the values to the given precision

$$\begin{aligned} F &= \{0.93, 1.01, 1.001, 3.02, 2.99, 5.03, 5.01, 4.98\} \\ \Rightarrow F_{smoothed} &= \{1.0, 1.0, 1.0, 3.0, 3.0, 5.0, 5.0, 5.0\} \end{aligned}$$

- The dimensionality of the data space (number of distinct examples) is also reduced at the same time

Differences and Ratios

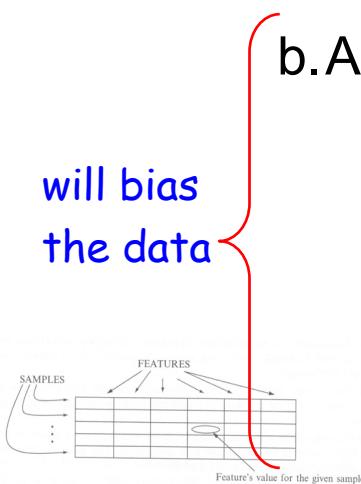
- Can be viewed as a kind of attribute/feature construction
 - New attributes are constructed from the given attributes
 - Can discover the missing information about the relationships between data attributes
 - Can be applied to the *input* and *output* features for data mining
- E.g.,
 1. Difference
 - E.g., “ $s(t+1) - s(t)$ ”, relative moves for control setting
 2. Ratio
 - E.g., “ $s(t+1) / s(t)$ ”, levels of increase or decrease
 - E.g., Body-Mass Index (BMI)
$$\frac{\text{Weight}(Kg)}{\text{Height}(m^2)}$$

Missing Data

- In real-world application, the subset of samples or future cases with complete data may be relatively small
 - Some data mining methods accept missing values
 - Others require all values be available
 - Try to drop the samples or fill in the missing attribute values in during data preparation

Missing Data (cont.)

- Two major ways to deal with missing data (values)
 1. Reduce the data set and eliminate all samples with missing values
 - If large data set available and only a small portion of data with missing values
 2. Find values for missing data
 - a. Domain experts examine and enter reasonable, probable, and expected values for the missing data
 - b. Automatically replace missing values with some constants
 - b.1 Replace a missing value with a single global constant
 - b.2 Replace a missing value with its feature mean
 - b.3 Replace a missing value with its feature mean for the given class (if class labeling information available)
 - b.4 Replace a missing value with the most probable value (e.g., according to the values of other attributes of the present data)



will bias
the data

Missing Data (cont.)

- The replaced value(s) (especially for b.1~b.3) will homogenize the cases / samples with missing values into an artificial class
- Other solutions
 1. “Don’t Care”
 - Interpret missing values as “don’t care” values
$$\vec{x} = \langle 1, ?, 3 \rangle, \text{ with feature values in domain } [0,1,2,3,4]$$
$$\Rightarrow \vec{x}_1 = \langle 1, 0, 3 \rangle, \vec{x}_2 = \langle 1, 1, 3 \rangle, \vec{x}_3 = \langle 1, 2, 3 \rangle, \vec{x}_4 = \langle 1, 3, 3 \rangle, \vec{x}_5 = \langle 1, 4, 3 \rangle$$
 - A explosion of artificial samples being generated !
 2. Generate multiple solutions of data-mining with and without missing-value features and then analyze and interpret them !

$$\begin{array}{c} A_1, B_1, C_1 \\ A_2, B_2, C_2 \\ \dots \qquad \Rightarrow (A, B, ?), (A, ?, C), (?, B, C) \\ A_N, B_N, C_N \end{array}$$

Time-Dependent Data

- Time-dependent relationships may exist in specific features of data samples
 - E.g., “temperature reading” and speech are a univariate time series, and video is a multivariate time series

$$X = \{t(0), t(1), t(2), t(3), t(4), t(5), t(6), t(7), t(8), t(9), t(10)\}$$

- Forecast or predict $t(n+1)$ from previous values of the feature

TABLE 2.1 Transformation of Time Series to standard tabular form (window = 5)

Sample	W I N D O W					Next Value
	M1	M2	M3	M4	M5	
1	t(0)	t(1)	t(2)	t(3)	t(4)	t(5)
2	t(1)	t(2)	t(3)	t(4)	t(5)	t(6)
3	t(2)	t(3)	t(4)	t(5)	t(6)	t(7)
4	t(3)	t(4)	t(5)	t(6)	t(7)	t(8)
5	t(4)	t(5)	t(6)	t(7)	t(8)	t(9)
6	t(5)	t(6)	t(7)	t(8)	t(9)	t(10)

Time-Dependent Data (cont.)

- Forecast or predict $t(n+j)$ from previous values of the feature

TABLE 2.2 Time-series samples in standard tabular form
(window = 5) with postponed predictions ($j = 3$)

Sample	W	I	N	D	O	W	Next Value
	M1	M2	M3	M4	M5		
1		$t(0)$	$t(1)$	$t(2)$	$t(3)$	$t(4)$	$t(7)$
2		$t(1)$	$t(2)$	$t(3)$	$t(4)$	$t(5)$	$t(8)$
3		$t(2)$	$t(3)$	$t(4)$	$t(5)$	$t(6)$	$t(9)$
4		$t(3)$	$t(4)$	$t(5)$	$t(6)$	$t(7)$	$t(10)$

- As mentioned earlier, forecast or predict the differences or ratios of attribute values
 - $t(n+1) - t(n)$
 - $t(n+1) / t(n)$

Time-Dependent Data (cont.)

- “Moving Averages” (MA)– a single average summarizes the most m feature values for each case at each time moment i
 - Reduce the random variation and noise components

$$MA(i, M) = \frac{1}{M} \cdot \sum_{j=i-M+1}^i t(j),$$

$t(j)$: noisy data, $\hat{t}(j)$: clean data

$t(j) = \hat{t}(j) + \text{error}$, error is assumed to be a constant

$$\Rightarrow \underline{MA(i, M)} = \frac{1}{M} \cdot \sum_{j=i-M+1}^i t(j) = \underline{\text{mean}(j) + \text{error}}$$

, where $\text{mean}(j) = \sum_{j=i-M+1}^i \hat{t}(j)$

$$\Rightarrow t(j) - MA(i, M) = \hat{t}(j) - \text{mean}(j)$$

Time-Dependent Data (cont.)

- “Exponential Moving Averages” (EMA) – give more weight to the most recent time periods

$$EMA(i, M) = p \cdot t(i) + (1 - p) \cdot EMA(i-1, M-1)$$

$$EMA(i, 1) = t(i)$$

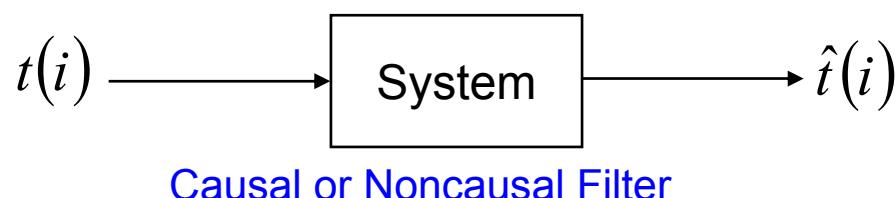
if $p = 0.5$

$$EMA(i, 2) = 0.5 \cdot t(i) + 0.5 \cdot EMA(i-1, 1)$$

$$EMA(i, 3) = 0.5 \cdot t(i) + 0.5 \cdot EMA(i-1, 2)$$

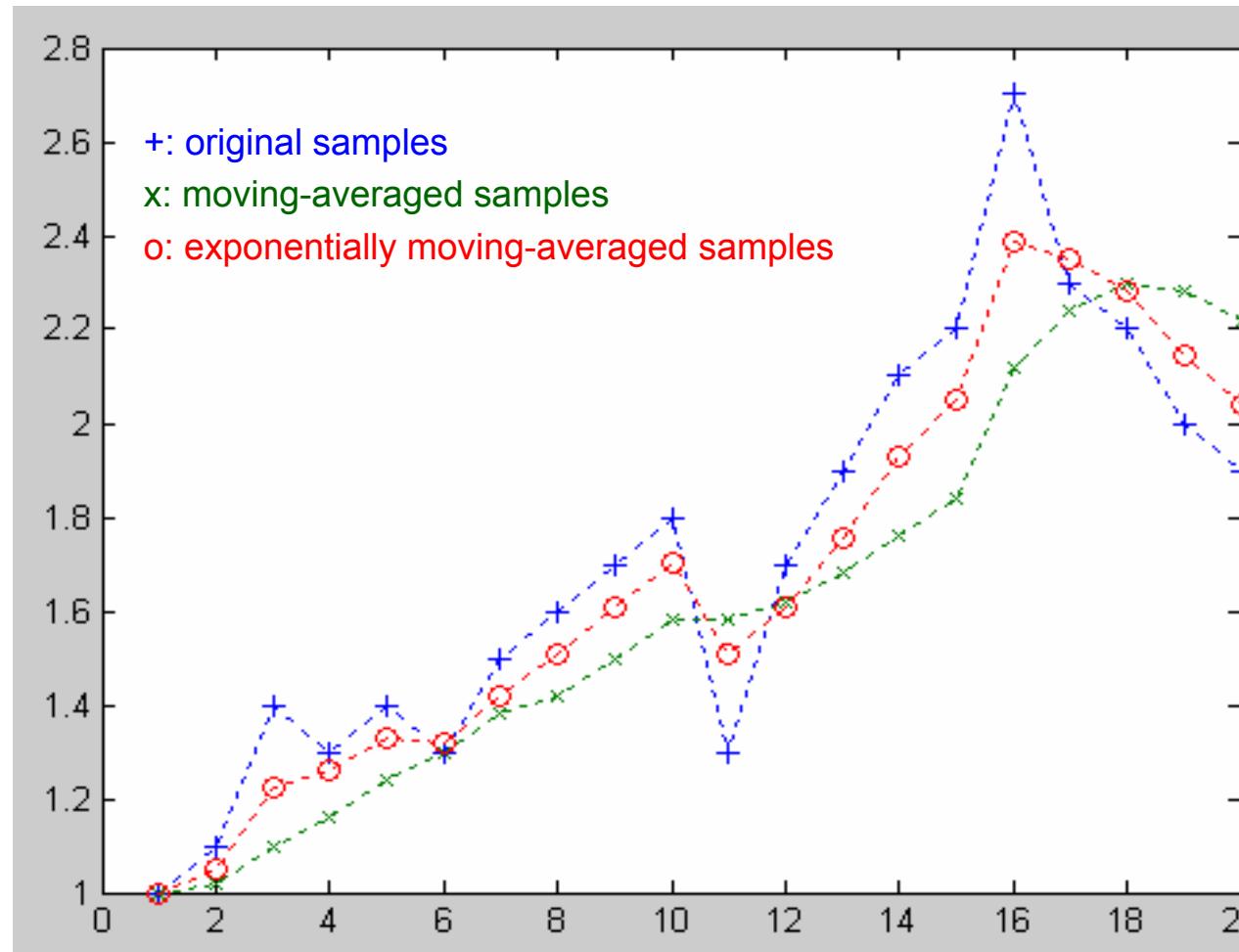
$$= 0.5 \cdot t(i) + 0.5 \cdot [0.5 \cdot t(i-1) + 0.5 \cdot EMA(i-2, 1)]$$

$$= 0.5 \cdot t(i) + 0.5 \cdot [0.5 \cdot t(i-1) + 0.5 \cdot t(i-2)]$$



Time-Dependent Data (cont.)

X=[1.0 1.1 1.4 1.3 1.4 1.3 1.5 1.6 1.7 1.8 1.3 1.7 1.9 2.1 2.2 2.7 2.3 2.2 2.0 1.9];



Time-Dependent Data (cont.)

- Appendix: *MATLab Codes for Moving Averages (MA)*

```
W=1:20;  
X=[1.0 1.1 1.4 1.3 1.4 1.3 1.5 1.6 1.7 1.8 1.3 1.7 1.9 2.1 2.2 2.7 2.3 2.2 2.0 1.9];  
U=zeros(5,20);  
  
for M=0:10  
    for i=1:20  
        sum=0.0;  
        for m=0:M  
            if i-m>0  
                sum=sum+X(i-m);  
            else  
                sum=sum+X(1);  
            end  
        end  
        U(M+1,i)=sum/(M+1);  
    end  
end  
plot(W,U(1,:),'+',W,U(5,:),'x');
```

Homework-1: Data Preparation

- Exponential Moving Averages (EMA)

X=[1.0 1.1 1.4 1.3 1.4 1.3 1.5 1.6 1.7 1.8 1.3 1.7 1.9 2.1 2.2 2.7 2.3 2.2 2.0 1.9];

$$EMA(i, m) = p \cdot t(i) + (1 - p) \cdot EMA(i - 1, m - 1)$$
$$EMA(i, 1) = t(i)$$

- Try out different settings of m and p
 - Discuss on the results you observed
 - Discuss the applications in which you would prefer to use exponential moving averages (EMA) instead of moving averages (MA)
-
- Due date: 2004/3/17

Time-Dependent Data (cont.)

- Example: multivariate time series

spatial information

Temporal information

→ → →

Time	a	b
1	5	117
2	8	113
3	4	116
4	9	118
5	10	119
6	12	120

Sample a(n-2) a(n-1) a(n) b(n-2) b(n-1) b(n)

Sample	a(n-2)	a(n-1)	a(n)	b(n-2)	b(n-1)	b(n)
1	5	8	4	117	113	116
2	8	4	9	113	116	118
3	4	9	8	116	118	119
4	9	10	12	118	119	120

cases ?
feature ?
values ?

date reduction

a) Initial time-dependent data

b) Samples prepared for data mining with time window = 3

FIGURE 2.3 Tabulation of time-dependent features a and b

High dimensions of data generated during the transformation of time-dependent can be reduced through "data reduction"

Outlier Analysis

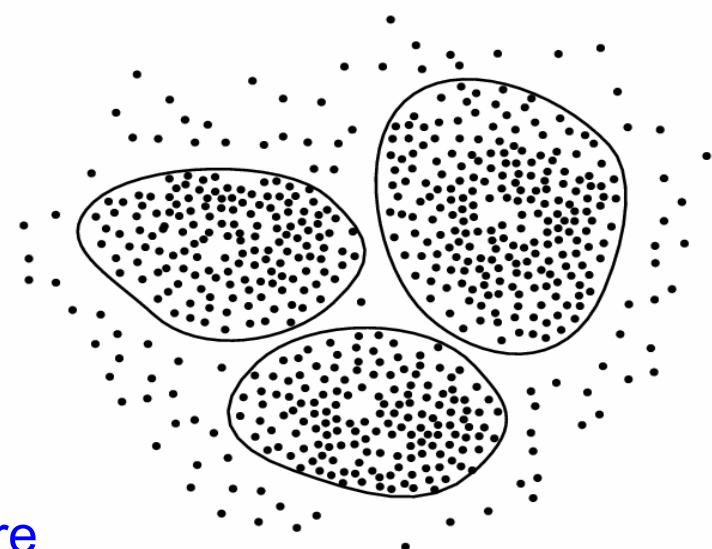
- Outliers
 - Data samples that do not comply with the general behavior of the data model and are significantly different or inconsistent with the remaining set of data
 - E.g., a person's age is “-999”, the number of children for one person is “25”, (typographical errors/typos)
- Many data-mining algorithms try to minimize the influence of outliers or eliminate them all together
 - However, it could result in the loss of important hidden information
 - “one person's noise could be another person's signal”, e.g., outliers may indicate abnormal activity

Outlier Analysis (cont.)

- Applications:
 - Credit card fraud detection
 - Telecom fraud detection
 - Customer segmentation
 - Medical analysis

Outlier Analysis (cont.)

- Outlier detection/mining
 - Given a set of n samples, and k , the expected number of outliers, find the top k samples that are considerably dissimilar, exceptional, or inconsistent with respect to the remaining data
 - Can be viewed as two subproblems
 - Define what can be considered as inconsistent in a given data set
 - Nontrivial
 - Find an efficient method to mine the outliers so defined
 - Three methods introduced here



Visual detection of outlier ?

Outlier Analysis (cont.)

1. Statistical-based Outlier Detection

- Assume a distribution or probability model for the given data set and then identifies outliers with respect to the model using a *discordance test*
 - Data distribution is given/assumed (e.g., normal distribution)
 - Distribution parameters: mean, variance
 - Threshold value as a function of variance

$Age = \{3, 56, 23, 39, 156, 52, 41, 22, 9, 28, 139, 31, 55, 20, -67, 37, 11, 55, 45, 37\}$

$Mean = 39.9$

$Standard deviation = 45.65$

$Threshold = Mean \pm 2 \times Standard deviation$

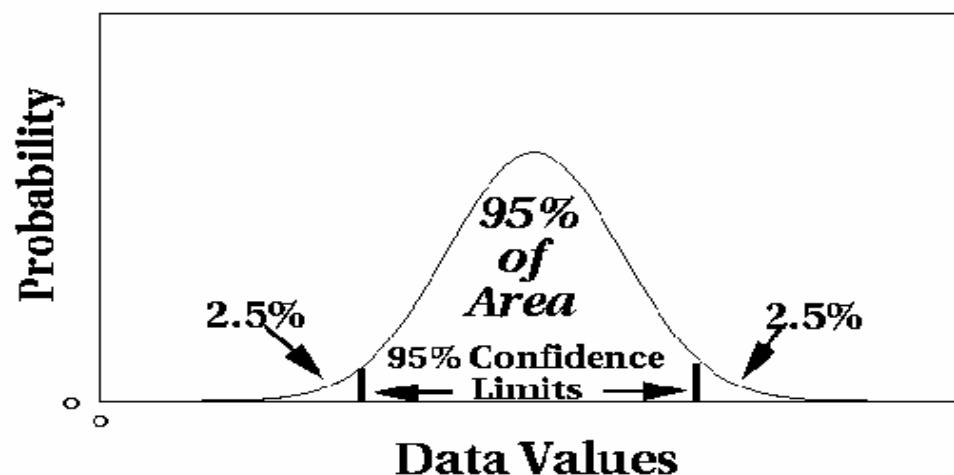
$[-54., 131.2] \Rightarrow [0, 131.2]$ Age is always greater than zero !

$\Rightarrow outliers : 156, 139, -67$

Outlier Analysis (cont.)

1. Statistical-based Outlier Detection (cont.)

- Drawbacks
 - Most tests are for single attribute
 - In many cases, data distribution may not be known



Outlier Analysis (cont.)

2. Distance-based Outlier Detection

- A sample s_i in a data S is an outlier if at least a fraction p of the objects in S lies at a distance greater than d , denoted as $DB<p, d>$

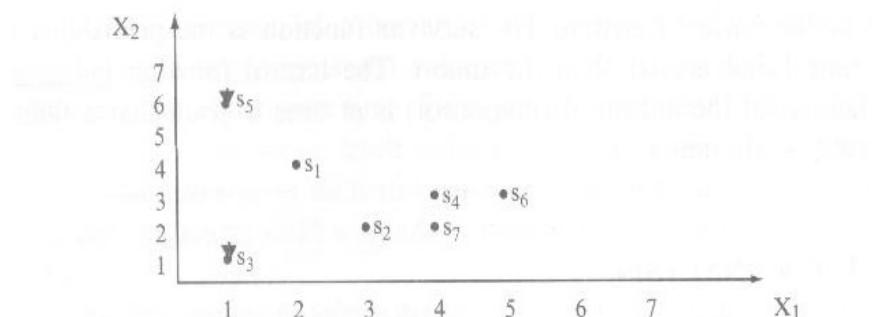


FIGURE 2.4 Visualization of two-dimensional data set for outlier detection

- If $DB<p, d>=DB<4, 3>$

$$d = \left[(x_1 - x_1)^2 + (y_1 - y_1)^2 \right]^{1/2}$$

- Outliers: s_3, s_5

TABLE 2.3 Table of distances for data set S

	s_1	s_2	s_3	s_4	s_5	s_6	s_7
s_1		2.236	3.162	2.236	2.236	3.162	2.828
s_2			2.236	1.414	4.472	2.236	1.000
s_3				3.605	5.000	4.472	3.162
s_4					4.242	1.000	1.000
s_5						5.000	5.000
s_6							1.414

the distance greater than d for each given point in S

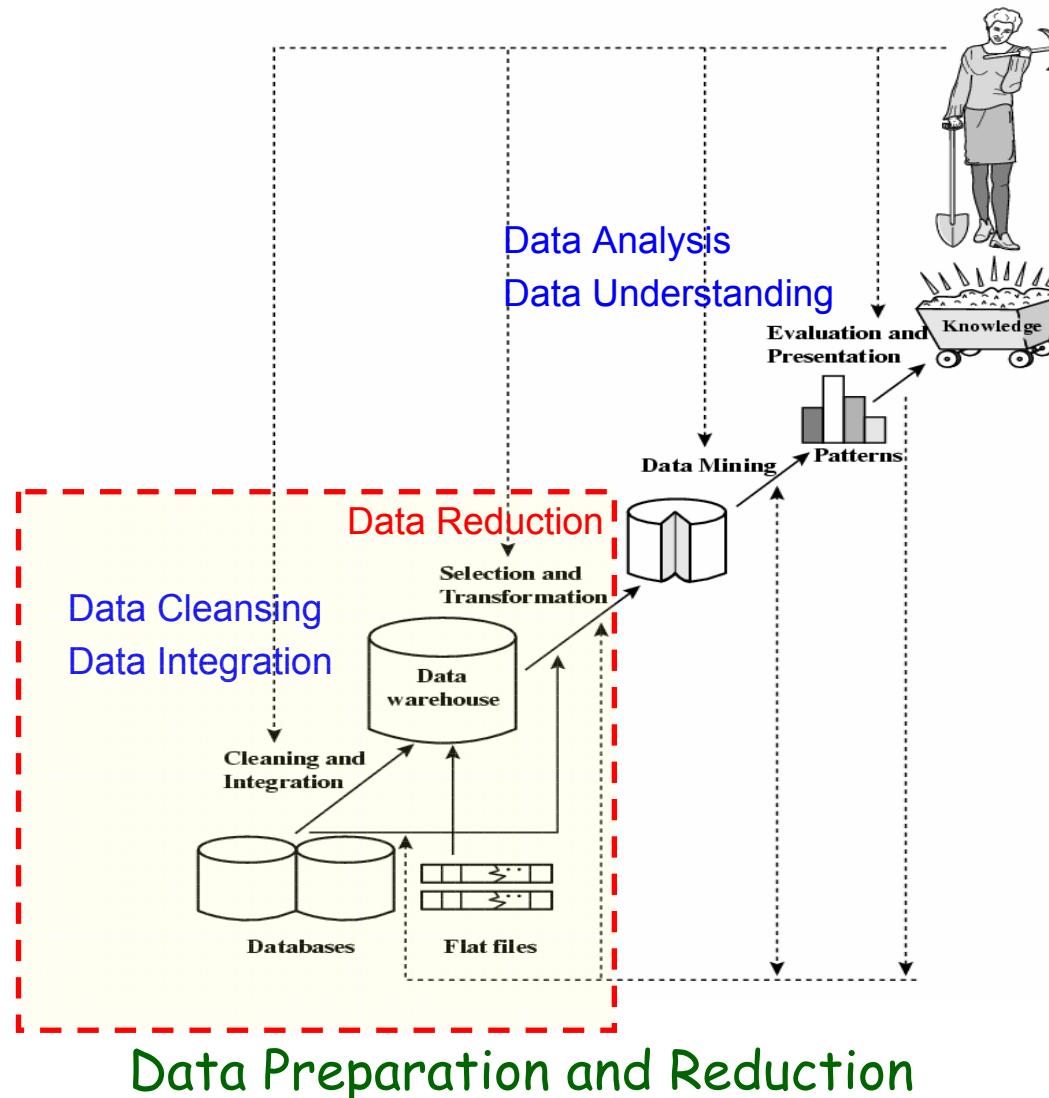
Sample	p
s_1	2
s_2	1
s_3	5
s_4	2
s_5	5
s_6	3

Outlier Analysis (cont.)

3. Deviation-based Outlier Detection

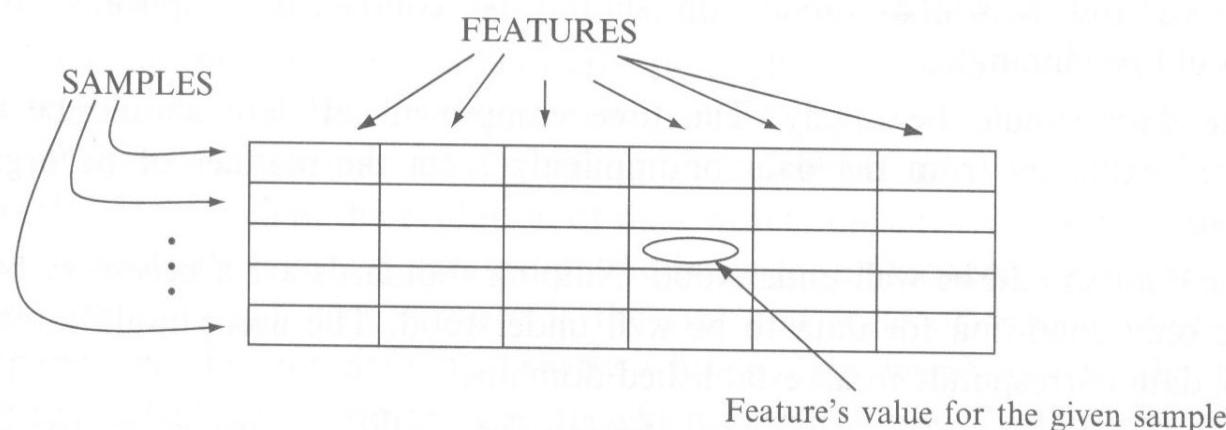
- Define the basic characteristics of the sample set, and all samples that deviate from these characteristics are outliers
- The “sequence exception technique”
 - Based on a dissimilarity function, e.g., variance $\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$
 - Find the smallest subset of samples whose removal results in the greatest reduction of the dissimilarity function for the residual set (a NP-hard problem)

Where Are We Now ?



Introduction to Data Reduction

- Three dimensions of data sets
 - Rows (cases, samples, examples)
 - **Columns (features)**
 - Values of the features
- We hope that the final reduction doesn't reduce the quality of results, instead the results of data mining can be even improved



Introduction to Data Reduction (cont.)

- Three basic operations in data reduction
 - Delete a column
 - Delete a row
 - Reduce the number of values in a column
- Gains or losses with data reduction
 - Computing time
 - Tradeoff existed for preprocessing and data-mining phases
 - Predictive/descriptive accuracy
 - Faster and more accurate model estimation
 - Representation of the data-mining model
 - Simplicity of model representation (model can be better understood)
 - Tradeoff between **simplicity** and **accuracy**

 Preserve the characteristic
of original data
 Delete the nonessential data

Introduction to Data Reduction (cont.)

- Recommended characteristics of data-reduction algorithms
 - Measure quality
 - Quality of approximated results using a reduced data set can be determined precisely
 - Recognizable quality
 - Quality of approximated results can be determined at preprocessing phase
 - Monotonicity
 - Iterative, and monotonically decreasing in time and quality
 - Consistency
 - Quality of approximated results is correlated with computation time and input data quality
 - Diminishing returns (Convergence)
 - Significant improvement in early iterations and which diminished over time
 - Interruptability
 - Can be stopped at any time and provide some answers
 - Preemptability
 - Can be suspended and resumed with minimal overhead

Feature Reduction

- Also called “column reduction”
 - Also have the side effect of case reduction
- Two standard tasks for producing a reduced feature set
 1. Feature selection
 - Objective: find a subset of features with performances comparable to the full set of features
 2. Feature composition (*do not discuss it here!*)
 - New features/attributes are constructed from the given/old features/attributes and those given ones are discarded later on !
 - For example $\frac{\text{Weight}(\text{Kg})}{\text{Height}(\text{m}^2)}$
 - » Body-Mass Index (BMI)
 - » New features/dimensions retained after principal component analysis (PCA)
 - Interdisciplinary approaches and domain knowledge

Feature selection (cont.)

- Select a subset of the features based domain knowledge and data-mining goals
- Can be viewed as a search problem
 - Manual or automated

Feature selection as searching
 $\{A_1, A_2, A_3\}$
⇒ $\{0,0,0\}, \{1,0,0\},$
 $\{0,1,0\}, \dots, \{1,1,1\}$
1: with the feature
0: without the feature

- Find optimal or near-optimal solutions (subsets of features) ?

Feature selection (cont.)

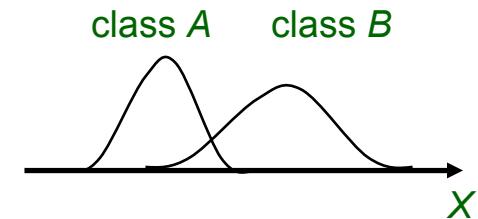
- Methods can be classified as
 - a. Feature ranking algorithms
 - b. Minimum subset algorithms
- Button-up: starts with an empty set and fill it in by choosing the most relevant features from the initial set of features
- Top-down: begin with a full set of original features and remove one-by-one those that are irrelevant
- Methods also can be classified as
 - a. Supervised : Use class label information
 - b. Unsupervised: Do not use class label information

Supervised Feature Selection (cont.)

- Method I: Simply based on comparison of means and variances
 - Assume the distribution of the feature forms a normal curve
 - Feature means of different categories/classes are normalized and then compared
 - If means are far apart → interest in a feature increases
 - If means are indistinguishable → interest wanes in that feature

$$SE(X_A - X_B) = \sqrt{\frac{var(X_A)}{n_{X,A}} + \frac{var(X_B)}{n_{X,B}}}$$

$$TEST : \frac{|mean(X_A) - mean(X_B)|}{SE(X_A - X_B)} > \text{threshold} - \text{value}$$



- Simple but effective
- Without taking into consideration relationship to other features
 - Assume features are independent of each other

Supervised Feature Selection (cont.)

- **Example:** threshold - value = 0.5

TABLE 3.1 Dataset with three features

X	Y	C
0.3	0.7	A
0.2	0.9	B
0.6	0.6	A
0.5	0.5	A
0.7	0.7	B
0.4	0.9	B



$$X_A = \{0.3, 0.6, 0.5\}, n_{X,A} = 3$$

$$X_B = \{0.2, 0.7, 0.4\}, n_{X,B} = 3$$

$$Y_A = \{0.7, 0.6, 0.5\}, n_{Y,A} = 3$$

$$Y_B = \{0.9, 0.7, 0.9\}, n_{Y,B} = 3$$

$$SE(X_A - X_B) = \sqrt{\frac{var(X_A)}{n_{X,A}} + \frac{var(X_B)}{n_{X,B}}} = \sqrt{\frac{0.0233}{3} + \frac{0.6333}{3}} = 0.4678$$

$$\frac{|mean(X_A) - mean(X_B)|}{SE(X_A - X_B)} = \frac{|0.4667 - 0.4333|}{0.4678} = 0.0735 < 0.5$$

$$SE(Y_A - Y_B) = \sqrt{\frac{var(Y_A)}{n_{Y,A}} + \frac{var(Y_B)}{n_{Y,B}}} = \sqrt{\frac{0.010}{3} + \frac{0.0133}{3}} = 0.0875$$

$$\frac{|mean(Y_A) - mean(Y_B)|}{SE(Y_A - Y_B)} = \frac{|0.600 - 0.8333|}{0.0875} = 2.6667 > 0.5$$



$$\bar{x} = mean(x) = \frac{\sum x}{n_x}$$

$$var(x) = \frac{\sum (x - \bar{x})^2}{n_x - 1}$$

Supervised Feature Selection (cont.)

- Example: (cont.)
 - X is a candidate for feature reduction
 - Y is significantly above the threshold value $\rightarrow Y$ has the potential to be a distinguishing feature between two classes
 - How to extend such a method to K -class problems
 - $k(k-1)/2$ pairwise comparisons are needed ?

Supervised Feature Selection (cont.)

- Method II: Features examined collectively instead of independently, additional information can be obtained

$C : m \times m$ covariance matrix, each entry $C_{i,j}$  m features are selected
stands for the correlation between two features i, j

$$C_{i,j} = \frac{1}{n} \sum_{k=1}^n (v(k,i) - m(i)) \cdot (v(k,j) - m(j))$$

 number of samples

$v(k,i)$: the value of feature i of sample k
 $m(i)$: mean of feature i

$$DM = (M_1 - M_2)(C_1 + C_2)^{-1}(M_1 - M_2)^T \quad \longleftarrow \quad \text{distance measure for multivariate variables}$$

- M_1, M_2, C_1, C_2 , are respectively mean vectors and covariance matrices for class 1 and class 2
- A subset set of features are selected for this measure (maximizing DM)
 - All subsets should be evaluated ! (how to do ? a combinatorial problem)

Review: Entropy

- Three interpretations for quantity of information
 1. The amount of **uncertainty** before seeing an event
 2. The amount of **surprise** when seeing an event
 3. The amount of **information** after seeing an event

- The definition of information:

define $0 \log_2 0 = 0$

$$I(x_i) = \log_2 \frac{1}{P(x_i)} = -\log_2 P(x_i)$$

– $P(x_i)$ the probability of an event x_i

- Entropy: the average amount of information

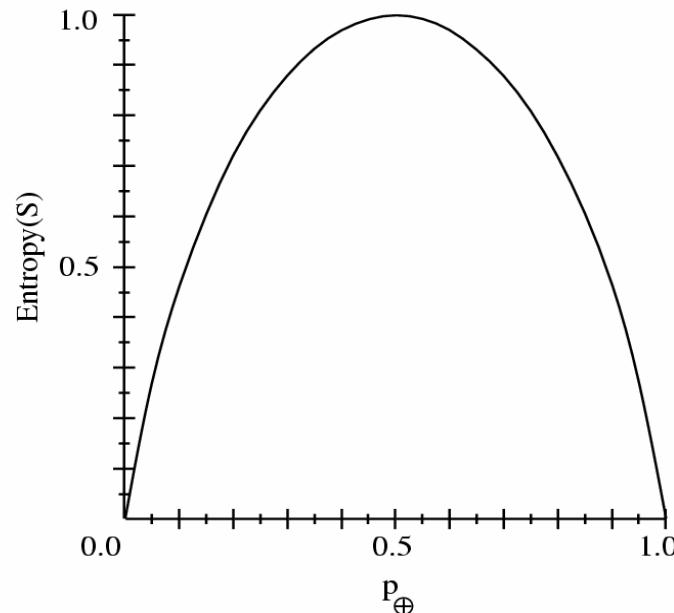
$$H(X) = E[I(X)]_X = E[-\log_2 P(x_i)]_X = \sum_{x_i} -P(x_i) \cdot \log_2 P(x_i)$$

– Have maximum value when the probability (mass) function is a uniform distribution

where $X = \{x_1, x_2, \dots, x_i, \dots\}$

Review: Entropy (cont.)

- For Boolean classification (0 or 1)



$$\text{Entropy}(X) = -p_1 \log_2 p_1 - p_2 \log_2 p_2$$

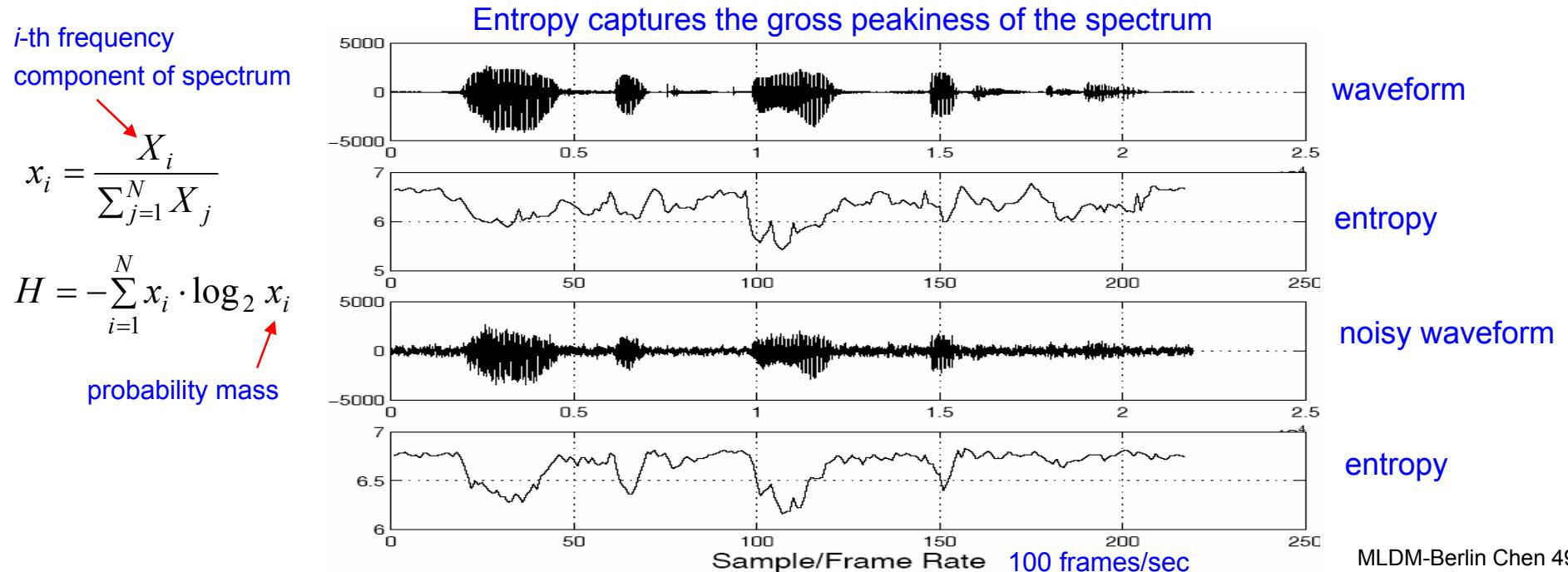
-相同機率分佈下(如Uniform)，event個數越多，entropy越大
 $(\frac{1}{2}, \frac{1}{2}) \rightarrow 1, (\frac{1}{4}, \frac{1}{4}, \frac{1}{4}, \frac{1}{4}) \rightarrow 2$
-event個數固定情況下，機率分佈越平均(如Uniform)，entropy越大

- Entropy can be expressed as the minimum number of bits of information needed to encode the classification of an arbitrary number of examples
 - If c classes are generated, the maximum of Entropy can be

$$\text{Entropy}(X) = \log_2 c$$

Review: Entropy (cont.)

- Illustrative Example
 - Discriminate speech portions from non-speech portions for Voice Activity Detection (VAD)
 - Speech has clear formants and entropies of such spectra will be slow
 - Non-speech has flatter spectra and the associated entropies should be higher



Unsupervised Feature Selection

- Method I: Entropy measure for ranking features
 - Assumptions
 - All samples are given as vectors of feature values **without any categorical information**
 - The removal of an irrelevant (redundant) feature may not change the basic characteristics of the data set
 - basic characteristics → the similarity measure between any pair of samples
 - Use **entropy** to observe the change of global information before and after removal of a specific feature
 - Higher entropy for disordered configurations
 - Less entropy for ordered configurations
 - Rank features by iteratively (gradually) removing the least important feature in maintaining the configuration order

Unsupervised Feature Selection (cont.)

- Method I: Entropy measure for ranking features (cont.)

- Distance measure between two samples x_i and x_j

$$D_{ij} = \left[\sum_{k=1}^n \left((x_{ik} - x_{jk}) / (\max_k - \min_k) \right)^2 \right]^{1/2}$$

number of features

- Change the distance measure to likelihood of proximity/similarity using exponential operator (function)

$$S_{ij} = \exp(-\alpha D_{ij})$$

α is simply set to 0.5
or is set as $-(\ln 0.5) / D_{average}$

ranging between 0 ~1

- $S_{ij} \approx 1$: x_i and x_j is very similar
 - $S_{ij} \approx 0$: x_i and x_j is very dissimilar

- For Categorical (nominal/nonmetric) features

- Hamming distance

$$S_{ij} = \left(\sum_{k=1}^n |x_{ik} = x_{jk}| \right) / n,$$

$|x_{ik} = x_{jk}| = 1 \text{ if } x_{ik} = x_{jk} \text{ and } 0 \text{ otherwise}$

ranging between 0 ~1

Unsupervised Feature Selection (cont.)

- Use entropy to monitor the changes in proximity between any sample pair in the data set (data set with size N)

$$E = \sum_{i=1}^{N-1} \sum_{j=i+1}^N H_{i,j}$$

$$= \sum_{i=1}^{N-1} \sum_{j=i+1}^N \left(S_{ij} \log S_{ij} + (1 - S_{ij}) \log (1 - S_{ij}) \right)$$

↑ Likelihood of being similar
↑ Likelihood of being dissimilar

- Example: a simple data set with three **categorical features**

Sample	F ₁	F ₂	F ₃
R ₁	A	X	1
R ₂	B	Y	2
R ₃	C	Y	2
R ₄	B	X	1
R ₅	C	Z	3

	R ₁	R ₂	R ₃	R ₄	R ₅
R ₁	0/3	0/3	2/3	0/3	
R ₂		2/3	1/3	0/3	
R ₃			0/3	1/3	
R ₄				0/3	

Data set

$$\text{e.g., } H_{1,2} = H_{2,1} = -[(0/3)\log(0/3) + (3/3)\log(3/3)]$$

$$H_{1,4} = H_{4,1} = -[(2/3)\log(2/3) + (1/3)\log(1/3)]$$

Table of similarity measures

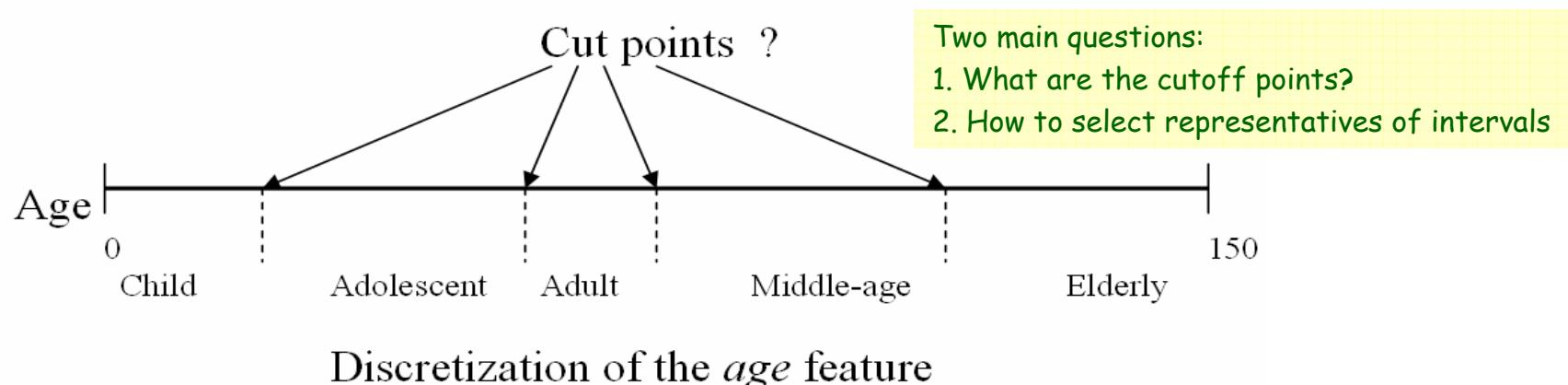
Unsupervised Feature Selection (cont.)

- Method I: Entropy measure for ranking features (cont.)
 - Algorithm
 1. Start with the initial set of features F
 2. For each feature f in F , remove f from F and obtain a subset F_f . Find the difference between entropy for F and F_f
$$|E_F - E_{F-f}|$$
 3. Find f_k such that its removal makes the entropy difference is minimum, check if the difference is less than the threshold
 4. If so, update the feature set as $F'=F- f_k$ and repeat steps 2~4 until only one feature is retained; otherwise, stop !

Disadvantage: the computational complexity is higher !

Value Reduction

- Also called Feature Discretization
- Goal: discretize the value of continuous features into a small number of intervals, where each interval is mapped to a discrete symbol
 - Simplify the tasks of data description and understanding
 - E.g., a person's age can be ranged from $0 \sim 150$
 - Classified into categorical segments:
“**child, adolescent, adult, middle age, elderly**”



Unsupervised Value Reduction

- Method I: Simple data reduction (value smoothing)

- Also called **number approximation by rounding**
 - Reduce the number of distinct values for a feature
 - E.g., round the values to the given precision

$$\begin{aligned}f &= \{0.93, 1.01, 1.001, 3.02, 2.99, 5.03, 5.01, 4.98\} \\ \Rightarrow f_{smoothed} &= \{1.0, 1.0, 1.0, 3.0, 3.0, 5.0, 5.0, 5.0\}\end{aligned}$$

- Properties
 - Each feature is smoothed independently of other features
 - Performed only once without iterations
 - The number of data samples (cases) may be also reduced at the same time

Unsupervised Value Reduction (cont.)

- Method II: Placing the value in bins
 - Order the numeric values using great-than or less-than operators
 - Partition the ordered value list into groups with close values
 - Also, these bins have close number of elements
 - All values in a bin is merged into a single concept represented by a single value, for example:
 - Mean or median/mode of the bin's value
 - The closest boundaries of each bin

$$f = \{3,2,1,5,4,3,1,7,5,3\}$$

ordering
 $\Rightarrow \{1,1,2,3,3,3,4,5,5,7\}$

splitting
 $\Rightarrow \{1,1,2 \quad 3,3,3 \quad 4,5,5,7\}$

Based on what criterion ?

Smoothing based on mean values $\Rightarrow \{1.33, 1.33, 1.33, 3, 3, 3, 5.25, 5.25, 5.25, 5.25\}$

Smoothing based on bin modes $\Rightarrow \{1, 1, 3, 3, 3, 5, 5, 5, 5\}$ replaced by the closest of

Smoothing based on boundary values $\Rightarrow \{1, 1, 2, 3, 3, 3, 4, 4, 7, 7\}$ the boundary values

Unsupervised Value Reduction (cont.)

- Method II: Placing the value in bins (cont.)
 - How to determine the optimal selection of k bins
 - Criterion: minimize the average distance of a value from its bin mean or median
 - Squared distance for a bin mean
 - Absolute distance for a bin median
 - Algorithm
 1. Sort all values for a given feature
 2. Assign approximately equal numbers of sorted adjacent value (v_i) to each bin, the number of bin is given in advance
 3. Move a border element v_i from one bin to the next (or previous) when that will reduce the global distance error (ER)

Unsupervised Value Reduction (cont.)

- Method II: Placing the value in bins (cont.)
 - Example

$$f = \{5, 1, 8, 2, 2, 9, 2, 1, 8, 6\}$$

ordering

$$\Rightarrow \{1, 1, 2, 2, 2, 5, 6, 8, 8, 9\}$$

splitting / Initializing

$$\Rightarrow \{1, 1, 2 \quad \boxed{2, 2, 5} \quad \boxed{6, 8, 8, 9}\}$$

....

$$\Rightarrow \{1, 1, 2, 2, 2 \quad 5, 6 \quad 8, 8, 9\}$$

\Rightarrow corresponding modes {2, 5, 8}

Absolute distance to bin modes

$$ER = (0 + 0 + 1) + (0 + 0 + 3) + (2 + 0 + 0 + 1) = 7$$

Absolute distance to bin modes

$$ER = (1 + 1 + 0 + 0 + 0) + (0 + 1) + (0 + 0 + 1) = 4$$

In real-world applications, the number of distinct values is controlled to be 50 ~ 100

Review: Chi-Square Test

- A non-parametric test of statistical significance for bivariate tabular analysis, which can provides degree of confidence in accepting or rejecting an hypothesis
 - E.g. (1), collocations in linguistics

dependent
variable/Categories

		$w_1 = \text{new}$	$w_1 \neq \text{new}$
Independent variable	$w_2 = \text{companies}$	8 (<i>new companies</i>)	4667 (<i>e.g., old companies</i>)
	$w_2 \neq \text{companies}$	15820 (<i>e.g., new machines</i>)	14287181 (<i>e.g., old machines</i>)

2x2 contingency table

A 2-by-2 table showing the dependence of occurrences of *new* and *companies*. There are 8 occurrences of *new companies* in the corpus, 4667 bigrams where the second word is *companies*, but the first word is not *new*, 15,820 bigrams with the first word *new* and a second word different from *companies*, and 14,287,181 bigrams that contain neither word in the appropriate position.

- Are “new” and “company” independent ?
 - Values of the independent variable has effect on the dependent variable?

Review: Chi-Square Test (cont.)

- E.g. (2), behavior analyses in sociology

Male and Female Footwear Preferences

dependent variable/Categorie *j*

Independent variable *i*

	Sandals	Sneakers	Leather shoes	Boots	Other	Total
Male	6	17	13	9	5	50
Female	13	5	7	16	9	50
Total	19	22	20	25	14	100

2x5 contingency table

- Biological sex and footwear preferences are independent ?
 - Values of the independent variable has effect on the dependent variable?

Ref: http://www.georgetown.edu/faculty/ballc/webtools/web_chi_tut.html

Review: Chi-Square Test (cont.)

- Null Hypothesis
 - In e.g. (2), biological sex and footwear preferences are independent

$$P(\text{male, Sandals}) = P(\text{male})P(\text{Sandals})$$

$$\Rightarrow N_{\text{male, Sandals}} = N \times P(\text{male})P(\text{Sandals})$$

$$\Rightarrow N_{\text{male, Sandals}} = N \times \frac{N_{\text{male}}}{N} \times \frac{N_{\text{Sandals}}}{N}$$

$$\Rightarrow N_{\text{male, Sandals}} = \frac{N_{\text{male}} \times N_{\text{Sandals}}}{N}$$

empirical frequency/count

$$O_{i,j}$$

expected frequency/count

$$E_{i,j}$$

	Sandals	Sneakers	Leather shoes	Boots	Other	Total
Male	6	17	13	9	5	50
Female	13	5	7	16	9	50
Total	19	22	20	25	14	100

$$\chi^2 = \sum_{i=1}^I \sum_{j=1}^J \frac{(O_{i,j} - E_{i,j})^2}{E_{i,j}}$$

with degrees of freedom = $(I - 1) \times (J - 1)$

which is more significant ?

$$(1005 - 1000)^2 > (13 - 10)^2$$

$$\frac{(1005 - 1000)^2}{1000} < \frac{(13 - 10)^2}{10}$$

Review: Chi-Square Test (cont.)

- Chi-Square Distribution

$$F_{\chi^2}(u, n) = \int_0^u \frac{x^{(n-2)/2} e^{-x/2} dx}{2^{n/2} [(n-2)/2]!}$$

$n \setminus F$.005	.010	.025	.050	.100	.250	.500	.750	.900	.950	.975	.990	.995
1	.0 ⁴ 393	.0 ³ 157	.0 ³ 982	.0 ² 393	.0158	.102	.455	1.32	<u>2.71</u>	3.84	5.02	6.63	7.88
2	.0100	.0201	.0506	.103	.211	.575	1.39	2.77	4.61	5.99	7.38	9.21	10.6
3	.0717	.115	.216	.352	.584	1.21	2.37	4.11	6.25	7.81	9.35	11.3	12.8
4	.207	.297	.484	.711	1.06	1.92	3.36	5.39	7.78	<u>9.49</u>	11.1	13.3	14.9
5	.412	.554	.831	1.15	1.61	2.67	4.35	6.63	9.24	<u>11.1</u>	12.8	15.1	16.7
6	.676	.872	1.24	1.64	2.20	3.45	5.35	7.84	10.6	12.6	14.4	16.8	18.5
7	.989	1.24	1.69	2.17	2.83	4.25	6.35	9.04	12.0	14.1	16.0	18.5	20.3
8	1.34	1.65	2.18	2.73	3.49	5.07	7.34	10.2	13.4	15.5	17.5	20.1	22.0
9	1.73	2.09	2.70	3.33	4.17	5.90	8.34	11.4	14.7	16.9	19.0	21.7	23.6
10	2.16	2.56	3.25	3.94	4.87	6.74	9.34	12.5	16.0	18.3	20.5	23.2	25.2
11	2.60	3.05	3.82	4.57	5.58	7.58	10.3	13.7	17.3	19.7	21.9	24.7	26.8
12	3.07	3.57	4.40	5.23	6.30	8.44	11.3	14.8	18.5	21.0	23.3	26.2	28.3
13	3.57	4.11	5.01	5.89	7.04	9.30	12.3	16.0	19.8	22.4	24.7	27.7	29.8
14	4.07	4.66	5.63	6.57	7.79	10.2	13.3	17.1	21.1	23.7	26.1	29.1	31.3
15	4.60	5.23	6.26	7.26	8.55	11.0	14.3	18.2	22.3	25.0	27.5	30.6	32.8
16	5.14	5.81	6.91	7.96	9.31	11.9	15.3	19.4	23.5	26.3	28.8	32.0	34.3
17	5.70	6.41	7.56	8.67	10.1	12.8	16.3	20.5	24.8	27.6	30.2	33.4	35.7
18	6.26	7.01	8.23	9.39	10.9	13.7	17.3	21.6	26.0	28.9	31.5	34.8	37.2
19	6.84	7.63	8.91	10.1	11.7	14.6	18.3	22.7	27.2	30.1	32.9	36.2	38.6
20	7.43	8.26	9.59	10.9	12.4	15.5	19.3	23.8	28.4	31.4	34.2	37.6	40.0
21	8.03	8.90	10.3	11.6	13.2	16.3	20.3	24.9	29.6	32.7	35.5	38.9	41.4
22	8.64	9.54	11.0	12.3	14.0	17.2	21.3	26.0	30.8	33.9	36.8	40.3	42.8
23	9.26	10.2	11.7	13.1	14.8	18.1	22.3	27.1	32.0	35.2	38.1	41.6	44.2
24	9.89	10.9	12.4	13.8	15.7	19.0	23.3	28.2	33.2	36.4	39.4	43.0	45.6
25	10.5	11.5	13.1	14.6	16.5	19.9	24.3	29.3	34.4	37.7	40.6	44.3	46.9
26	11.2	12.2	13.8	15.4	17.3	20.8	25.3	30.4	35.6	38.9	41.9	45.6	48.3
27	11.8	12.9	14.6	16.2	18.1	21.7	26.3	31.5	36.7	40.1	43.2	47.0	49.6
28	12.5	13.6	15.3	16.9	18.9	22.7	27.3	32.6	37.9	41.3	44.5	48.3	51.0
29	13.1	14.3	16.0	17.7	19.8	23.6	28.3	33.7	39.1	42.6	45.7	49.6	52.3
30	13.8	15.0	16.8	18.5	20.6	24.5	29.3	34.8	40.3	43.8	47.0	50.9	53.7

Review: Chi-Square Test (cont.)

- Chi-Square Distribution (cont.)
 - An asymmetric distribution

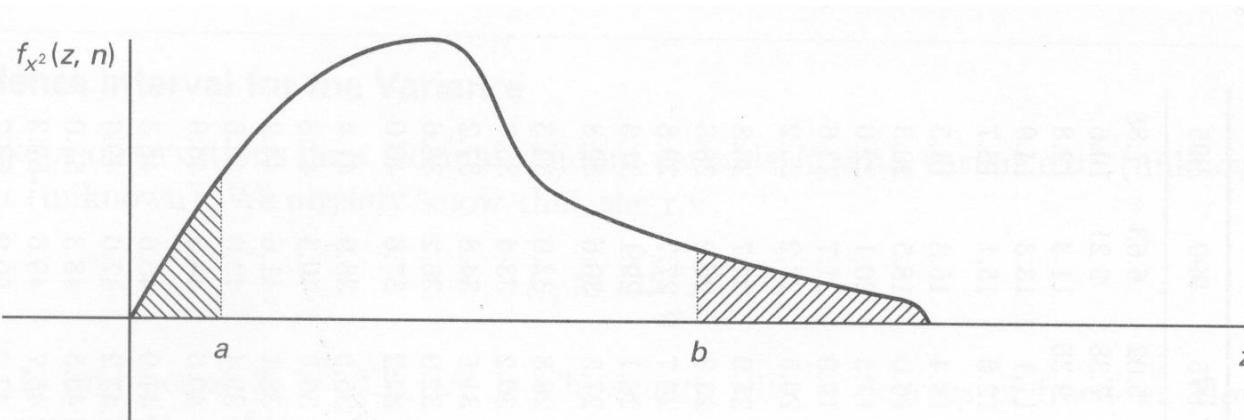


Figure 4.8-2 The points a, b are chosen so that equal amounts of area are removed from the tails. The area of the remainder should equal γ , the confidence level.

- In e.g. (2), for example, we can find $\chi^2 > u$ such that we can have a confidence of $P\%$ (or have error less than $100\% - P\%$) to reject the Null Hypothesis

Review: Chi-Square Test (cont.)

- E.g. (2), behavior analyses in sociology (cont.)

Table 1.e. Male and Female Undergraduate Footwear Preferences: Observed and Expected Frequencies

	Sandals	Sneakers	Leather shoes	Boots	Other	Total
Male observed	6	17	13	9	5	50
Male expected	9.5	11	10	12.5	7	
Female observed	13	5	7	16	9	50
Female expected	9.5	11	10	12.5	7	
Total	19	22	20	25	14	100

$$\begin{aligned} \text{Male/Sandals: } & ((19 \times 50)/100) = 9.5 \\ \text{Male/Sneakers: } & ((22 \times 50)/100) = 11 \\ \text{Male/Leather Shoes: } & ((20 \times 50)/100) = 10 \\ \text{Male/Boots: } & ((25 \times 50)/100) = 12.5 \\ \text{Male/Other: } & ((14 \times 50)/100) = 7 \end{aligned} \quad \left. \begin{aligned} \text{Female/Sandals: } & ((19 \times 50)/100) = 9.5 \\ \text{Female/Sneakers: } & ((22 \times 50)/100) = 11 \\ \text{Female/Leather Shoes: } & ((20 \times 50)/100) = 10 \\ \text{Female/Boots: } & ((25 \times 50)/100) = 12.5 \\ \text{Female/Other: } & ((14 \times 50)/100) = 7 \end{aligned} \right\}$$



$$\begin{aligned} \text{Male/Sandals: } & ((6 - 9.5)^2/9.5) = 1.289 \\ \text{Male/Sneakers: } & ((17 - 11)^2/11) = 3.273 \\ \text{Male/Leather Shoes: } & ((13 - 10)^2/10) = 0.900 \\ \text{Male/Boots: } & ((9 - 12.5)^2/12.5) = 0.980 \\ \text{Male/Other: } & ((5 - 7)^2/7) = 0.571 \\ \text{Female/Sandals: } & ((13 - 9.5)^2/9.5) = 1.289 \\ \text{Female/Sneakers: } & ((5 - 11)^2/11) = 3.273 \\ \text{Female/Leather Shoes: } & ((7 - 10)^2/10) = 0.900 \\ \text{Female/Boots: } & ((16 - 12.5)^2/12.5) = 0.980 \\ \text{Female/Other: } & ((9 - 7)^2/7) = 0.571 \end{aligned}$$

The total chi square value for Table 1 is 14.026.

The degrees of freedom for this Chi-Square distribution is $(2-1) \times (5-1) = 4$

Notice that because we originally obtained a balanced male/female sample, our male and female expected scores are the same.

Review: Chi-Square Test (cont.)

- E.g. (2), behavior analyses in sociology (cont.)
 - If we want to reject the Null Hypothesis with confidence larger than 95%, χ^2 must be larger than 9.49 (with degrees of freedom=4)
 - Because $14.2602 > 9.49$, we can reject the null hypothesis and affirm the claim that males and females differ in their footwear preferences

Supervised Value Reduction

- Method III: ChiMerge technique
 - An automated discretization algorithm that analyzes the quality of multiple intervals for a given feature using χ^2 statistics
 - Determine similarities between distributions of data in two adjacent intervals **based on output classification of samples**
 - If the χ^2 test indicates that the output class is independent of the feature's intervals, merge them; otherwise, stop merging!

Data Set	Sample: F	K
1	1	1
2	3	2
3	7	1
4	8	1
5	9	1
6	11	2
7	23	2
8	37	1
9	39	2
10	45	1
11	46	1
12	59	1

initial interval points :
0, 2, 5, 7.5, 8.5, 10, ..., 60

Supervised Value Reduction (cont.)

- Method III: ChiMerge technique (cont.)
 - Algorithm
 1. Sort the data for the given feature in ascending order
 2. Define initial intervals so that every value of the feature is in a separate interval
 3. Repeat until no χ^2 of any two adjacent intervals is less than threshold value
 - If no merge is possible, we can increase threshold value in order to increase the possibility of a new merge

Supervised Value Reduction (cont.)

- Method III: ChiMerge technique (cont.)

Data Set	Sample	F	K
1	1	1	
2	3	2	
3	7	1	
4	8	1	
5	9	1	
6	11	2	
7	23	2	
8	37	1	
9	39	2	
10	45	1	
11	46	1	
12	59	1	

initial interval points :

0, 2, 5, 7.5, 8.5, 10, ..., 60

$$\chi^2 = \sum_{i=1}^2 \sum_{j=1}^k (A_{ij} - E_{ij})^2 / E_{ij}$$

where:

$O_{i,j}$

k = number of classes,

A_{ij} = number of instances in the i -th interval, j -th class,

E_{ij} = expected frequency of A_{ij} , which is computed as $(R_i \cdot C_j) / N$,

R_i = number of instances in the i -th interval = $\sum A_{ij}$, $j = 1, \dots, k$,

C_j = number of instances in the j -th class = $\sum A_{ij}$, $i = 1, 2$,

N = total number of instances = $\sum R_i$, $i = 1, 2$.

χ^2 was minimum for intervals: [7.5, 8.5] and [8.5, 10]

	K=1	K=2	Σ
Interval [7.5, 8.5]	$A_{11}=1$	$A_{12}=0$	$R_1=1$
Interval [8.5, 9.5]	$A_{21}=1$	$A_{22}=0$	$R_2=1$
Σ	$C_1=2$	$C_2=0$	$N=2$

Based on the table's values, we can calculate expected values:

$$E_{11} = 2/2 = 1,$$

$$E_{12} = 0/2 \approx 0.1,$$

$$E_{21} = 2/2 = 1, \text{ and}$$

$$E_{22} = 0/2 \approx 0.1$$

and corresponding χ^2 test:

$$\chi^2 = (1 - 1)^2 / 1 + (0 - 0.1)^2 / 0.1 + (1 - 1)^2 / 1 + (0 - 0.1)^2 / 0.1 = 0.2$$

For the degree of freedom $d=1$, and $\chi^2 = 0.2 < 2.706$
(MERGE !)

degrees of freedom = $(I-1) \times (J-1)$

confidence > 0.90

Supervised Value Reduction (cont.)

- Method III: ChiMerge technique (cont.)

	K=1	K=2	Σ
Interval [0, 7.5]	A ₁₁ =2	A ₁₂ =1	R ₁ =3
Interval [7.5, 10]	A ₂₁ =2	A ₂₂ =0	R ₂ =2
Σ	C ₁ =4	C ₂ =1	N=5



	K=1	K=2	Σ
Interval [0, 10.0]	A ₁₁ =4	A ₁₂ =1	R ₁ =5
Interval [10.0, 42.0]	A ₂₁ =1	A ₂₂ =3	R ₂ =4
Σ	C ₁ =5	C ₂ =4	N=9

$$E_{11} = 12/5 = 2.4, \\ E_{12} = 3/5 = 0.6, \\ E_{21} = 8/5 = 1.6, \text{ and} \\ E_{22} = 2/5 = 0.4$$

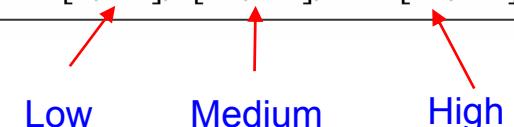
$$\chi^2 = (2 - 2.4)^2 / 2.4 + (1 - 0.6)^2 / 0.6 + (2 - 1.6)^2 / 1.6 + (0 - 0.4)^2 / 0.4$$

$$\chi^2 = 0.834$$

For the degree of freedom d=1, $\chi^2 = 0.834 < 2.706$ (MERGE!)

$E_{11} = 2.78, E_{12} = 2.22, E_{21} = 2.22, E_{22} = 1.78$, and $\chi^2 = 2.72 > 2.706$
(NO MERGE !)

Final discretization: [0, 10], [10, 42], and [42, 60]



Case Reduction

- Also called “raw reduction”
- Premise: the largest and the most critical dimension in the initial data set is the number of cases or samples
 - The number of rows in the tabular representation of data
- Simple case reduction can be done in the preprocessing (data-cleansing) phase
 - Elimination of outliers
 - Elimination of samples with missing feature values
- Or, case reduction achieved by using a sampled subset of samples (**called an estimator**) to provide some information about the entire data set (**using sampling methods**)
 - Reduced cost, greater speed, greater scope, even higher accuracy ?
 - Greater scope? can cover equally the rarely and frequently occurred samples

} There will be many samples remained !

estimator ?
estimate ?
estimation ?

Case Reduction (cont.)

- Method I: Systematic sampling
 - The simplest sampling technique
 - If 50% of a data set should be selected, simply take every other sample in a data set (e.g., 任兩個samples取其一)
 - There will be a problem, if the data set posses some regularities

$$D = \{(x^1, A), (x^2, B), (x^3, A), (x^4, B), (x^5, A), \dots, (x^N, B)\}$$

Sampling

\Rightarrow

$$D' = \{(x'^1, A), (x'^2, A), \dots, (x'^{N/2}, A)\}$$

Case Reduction (cont.)

- Method II: Random sampling
 - Every sample from the initial data set has the same chance of being selected in the subset
 - Two variants:
 1. Random sampling without replacement
 - Select n distinct samples from N initial samples without repetition
 - Avoid any bias in a selection
 2. Random sampling with replacement
 - All samples are given really equal chance of being selected, any of samples can be selected more than once

Case Reduction (cont.)

- Method II: Random sampling (cont.)
 - Notice that random sampling is an iterative process which may have two forms
 1. Incremental sampling 10%, 20%, 33%, 50%, 67%, 100%
 - Perform data mining on increasing larger random subsets to observe the trends in performances
 - The smallest subset should be substantial (e.g., >1000 samples)
 - Stop when no progress is made
 2. Average sampling
 - Solutions found from many random subsets of samples are averaged or voted
 - Regression problems → averaging
 - Classification problems → voting
 - Drawback: the repetitive process of data mining on smaller sets of samples

$$h_1(x) = A, h_2(x) = B, h_3(x) = A$$

$$\stackrel{\text{Voted}}{\Rightarrow} h^*(x) = A$$

$$h_1(x) = 6, h_2(x) = 6.5, h_3(x) = 6.7$$

$$\stackrel{\text{Averaged}}{\Rightarrow} h^*(x) = 6.4$$

Case Reduction (cont.)

- Method III: Stratified(分層的) sampling
 - The entire data set is split into non-overlapping subsets or strata
 - Sampling is performed for each different strata independently of each other
 - Combine all small subsets from different strata to form the final, total subset of samples
 - Better than random sampling if the strata is relatively homogeneous (\rightarrow smaller variance of sampled data)



- Method IV: Inverse sampling
 - Used when a feature in a data set occurs with rare frequency
(not enough information can be given to estimate a feature value)
 - Sampling start with the smallest subset and it continues until some conditions about the required number of feature values are satisfied

Data sampling for speech recognition “utterance-陳水扁” >10 times

“utterance-陳水在” >10 times

....

“utterance-陳萬水” >10 times

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HW-2-A: Feature Selection (Due 3/24)

- Unsupervised Feature Selection using Entropy Measure
 - Given four-dimensional samples where features are categorical:

X ₁	X ₂	X ₃	X ₄
3	3	1	A
3	6	2	A
5	3	1	B
5	6	2	B
7	3	1	A
5	4	2	B

Apply a method for unsupervised feature selection based on entropy measure to reduce one dimension from the given data set

HW-2-B: Value Reduction (Due 3/24)

- Supervised Value Reduction using ChiMerge
 - Given the data set X with two input features (I_1 and I_2) and one output feature (O) representing the classification of samples:

X:	I_1	I_2	O
	2.5	1.6	0
	7.2	4.3	1
	3.4	5.8	1
	5.6	3.6	0
	4.8	7.2	1
	8.1	4.9	0
	6.3	4.8	1

Apply ChiMerge to reduce the number of values (with confidence >0.9)

- Reduce the number of numeric values for feature I_1 and find the final, reduced number of intervals
- Reduce the number of numeric values for feature I_2 and find the final, reduced number of intervals